

# Word analysis prediction based on ARIMA model

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**Abstract.** First, Data processing was first performed to judge outliers if they were outliers, and finally missing values were filled in, and for the remaining valid data, change trend graphs were drawn to judge the trend of change in ascending rates and to predict future trends, using three mathematical models, ARIMA model, principal component analysis and Lasso regression model, which were used to describe the past change trends, and predict the level of change in the number of future word predictions. A comparative analysis of the models used above was conducted to compare the accuracy of each model, to derive which model predicted the most accurately, to give a rationale for the analysis, and to compare the accuracy of each model. Second, a model was built to analyze whether the change in the number of correct word predictions was related to which attributes of the words themselves and to elaborate the relationship. The data were subjected to KMO and Bartlett's tests to determine if a principal component analysis could be performed. This is followed by an exploration of whether the attribute has an effect on the number of correct predictions, how the change is affected, a visual presentation in the form of a graph, and a conclusion. To present an opinion, the paper considered the main factor that affects the number of predictions and propose measures to reduce the scenario brought by this factor. Finally, the paper came up a constructive report with listing and describing some other interesting features of this dataset.

**Keywords:** ARIMA model, Prediction Model, Lasso regression model, principal component analysis.

## 1. Introduction

Wordle is a popular puzzle currently offered daily by The New York Times. Players try to solve the puzzle by guessing a five-letter word in six or fewer attempts, receiving feedback for each guess. For this version, each guess must be an actual English word. Guesses that are not recognized as words by the game are not allowed. Wordle is growing in popularity and versions of the game now support over 60 languages.

The Wordle instructions on the New York Times website explain that the color of the block will change after you submit the word. A yellow square means that the letter in that square is in the word but in the wrong place. A green square means that the letter in the block is in the word and in the correct position. A gray square means that the letter in the square is not included in the word at all. Players can play in either regular mode or "hard mode". Wordle's Hard Mode makes the game more difficult by requiring players to use the correct letters (yellow or green squares) in subsequent guesses once they find them in a word.

The total number of entries is given in the dataset, and the content number is proportional to the growth of the date. Therefore, the content number can be used to predict the trend of a series instead of the date, and the trend of the data is statistical every day, so it can be considered a time series. The question required that given a word, and then predict the distribution of the reported results, where the impact indicators is needed to find, the first step is to study the correlation that requires quantification, factor analysis or principal component analysis method can be used for some data visualization analysis, etc., to facilitate the discovery of data relationships. And can be combined with the results of the previous three questions to analyze. In addition to the model, there must be some visualization results, and this part can be considered to output the results after each layer of attention into the form of heat map, which can reflect the process of feature extraction of words by. The number

of Wordle reports can reflect the size of the fan base of the game, and the popularity trend of the game can be observed. Roughly in January and February the number of fans grows rapidly, open questions, and some other features are derived.

## 2. Model Assumptions and Symbol Description

### 2.1. Model Assumptions

Hypothesis 1: Remove non-5-letter words. According to the question, only 5-letter words will appear in the game.

Hypothesis 2: Remove the data whose sum of percentages of attempts is not in the interval [99%,101%], beyond which the data is calculated incorrectly.

Hypothesis 3: Assume that measurement errors in available data are not considered.

### 2.2. Symbol Description

**Table 1.** Symbol Description

| Symbols    | Meaning                                                 |
|------------|---------------------------------------------------------|
| $O_i$      | Actual frequency                                        |
| $E_i$      | Expected frequency                                      |
| $\gamma^2$ | Cardinality                                             |
| $\mu$      | Average value                                           |
| $\sigma$   | Variance                                                |
| $SK$       | Skewness                                                |
| $K$        | Kurtosis                                                |
| $C_v$      | Coefficient of variation                                |
| $w$        | Weight values from input layer to hidden layer          |
| $b$        | Offset top of input layer to hidden layer               |
| $w'$       | Weight values from the hidden layer to the output layer |
| $b'$       | Offset top of hidden layer to output layer              |
| $\eta$     | Eigenvalue contribution rate                            |
| $r_{0i}$   | Relevance                                               |
| $O_i$      | Actual frequency                                        |

## 3. Modeling and solving the problem

### 3.1. Modeling and Solving Problem 1

#### 3.1.1 Modeling ideas

According to the statistics, there were 258 words with no repetition letters, 83 words with two identical letters (letter repeated once), and 2 words with three identical letters (letter replace twice) in the first classification. In the second classification, there were 25 words with a word frequency of five, 53 with a word frequency of four, 92 with a word frequency of three, 133 with a word frequency of two, 36 with a word frequency of one, and 6 that were not recorded (word frequency set to zero). We summed the reported percentage of scores for each type of word and averaged them.

#### 3.1.2 Model Building

In the use of many time series models, such as ARMA, ARIMA, will require that the time series is smooth, so generally in the study of a period of time series, the first step is required to conduct a smoothness test, in addition to the naked eye test method, in addition to the more commonly used rigorous statistical test is the ADF test, also called the unit root test. First, using the unit root test, determine whether the time series is smooth.

1. By analyzing the t-values, it was analyzed whether it could significantly reject the original hypothesis of series non-smoothness ( $p < 0.05$ ).

2. If it is significant, it indicates that the original hypothesis that the series is not smooth is rejected and the series is a smooth time series.

3. If it is not significant, it indicates that the original hypothesis that the series is not smooth cannot be rejected and the series is an unstable time series, and differencing of the data is considered, generally not exceeding second order differencing.

The ARIMA model requires the series to satisfy smoothness, view the ADF test results, and analyze whether it can significantly reject the hypothesis that the series is not smooth ( $p < 0.05$ ) based on the analyzed t-value. View the data comparison graph before and after differencing to determine whether it is smooth (not much up and down fluctuation), while the time series is biased (autocorrelation analysis), and its p and q values are estimated according to the truncated tail. ARIMA model requires the model to have pure randomness, that is, the model residuals are white noise, view the model test table, and test the model white noise according to the P value of Q statistic ( $P > 0.05$ ), also can be combined with the information criterion AIC and BIC values for analysis (the lower the better), but also through the model residuals ACF/PACF chart for analysis according to the model parameters table, the model formula combined with the time series analysis chart for comprehensive analysis, to obtain the backward prediction of the order results.

### 3.1.3 Model solving

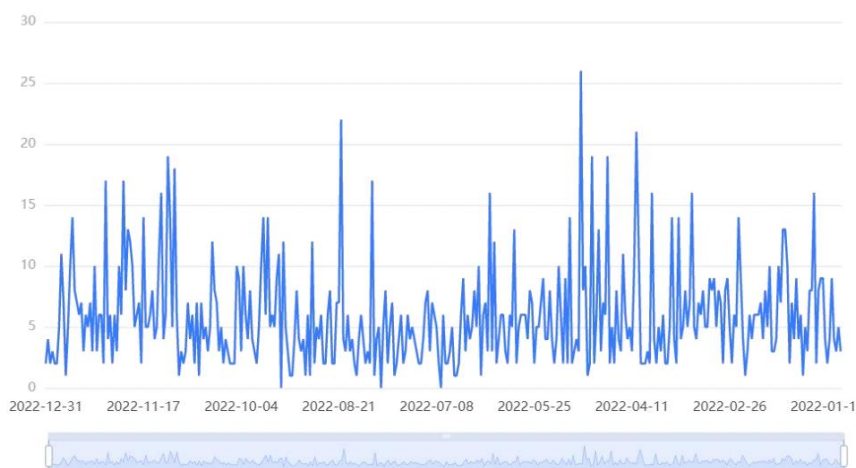
**Table 2.** ADF test table

| ADF Inspection Form |                  |         |          |          |           |       |        |
|---------------------|------------------|---------|----------|----------|-----------|-------|--------|
| Variables           | Difference order | t       | P        | AIC      | Threshold |       |        |
|                     |                  |         |          |          | 1%        | 5%    | 10%    |
| 2 tries             | 0                | -18.444 | 0.000*** | 1933.657 | -3.449    | -2.87 | -2.571 |
|                     | 1                | -9.185  | 0.000*** | 1961.841 | -3.449    | -2.87 | -2.571 |
|                     | 2                | -9.666  | 0.000*** | 2011.42  | -3.45     | -2.87 | -2.571 |

Note: \*\*\*, \*\*, \* represent 1%, 5%, 10% significance levels, respectively

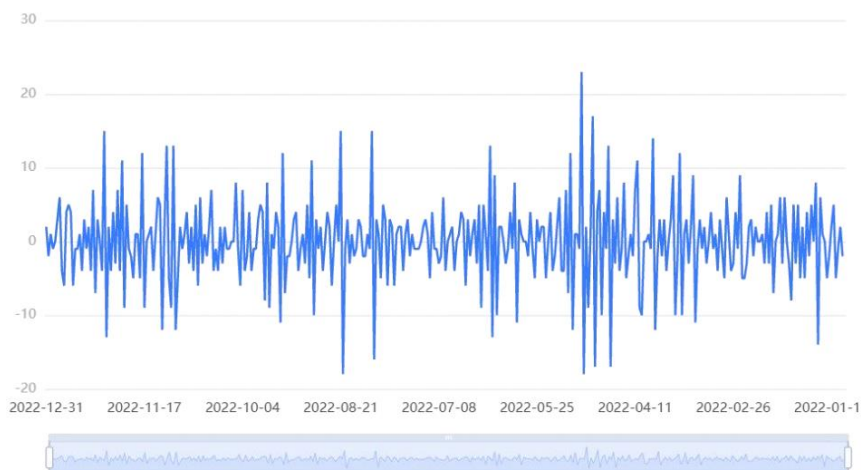
The above table shows the results of the ADF test, including variables, difference orders, t-test results, and AIC values, which are used to test whether the time series is smooth.

The results of this series test show that based on the variable 2 tries, the significance p-value is 0.000\*\*\* at the difference of order 0, which presents significance at the level and the original hypothesis is rejected, the series is a smooth time series.



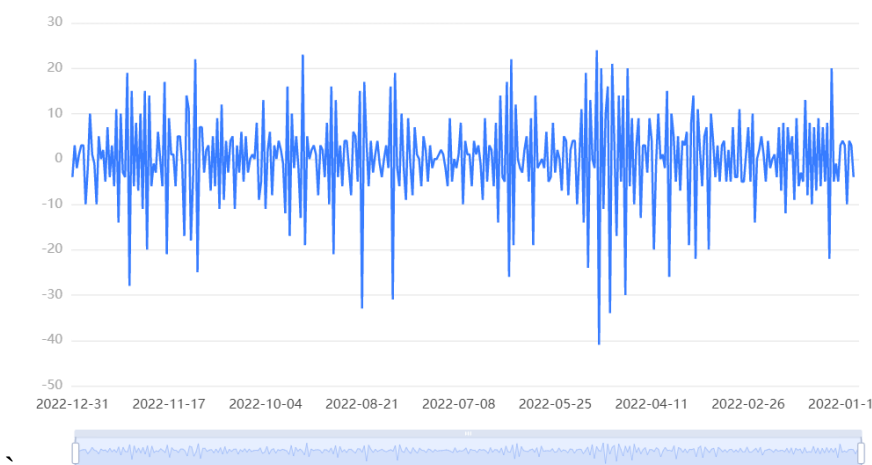
**Figure 1.** Original sequence diagram

The above figure shows the original plot without differencing.



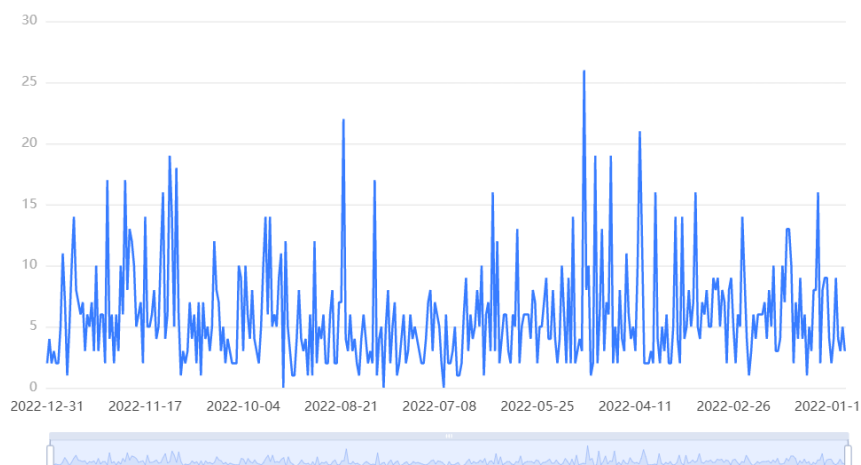
**Figure 2.** First-order difference diagram

The figure above shows a graph of the results of performing a first-order difference. When the time spacing is equal, the next value, minus the previous value, is used to obtain the first-order difference.



**Figure 3.** Second-order difference diagram

The figure above shows the result of performing a second-order difference. Doing the same thing twice, i.e., subtracting the last value from the first-order difference once more, is called "second-order difference".



**Figure 4.** Diagram of the best differential sequence of the second attempt



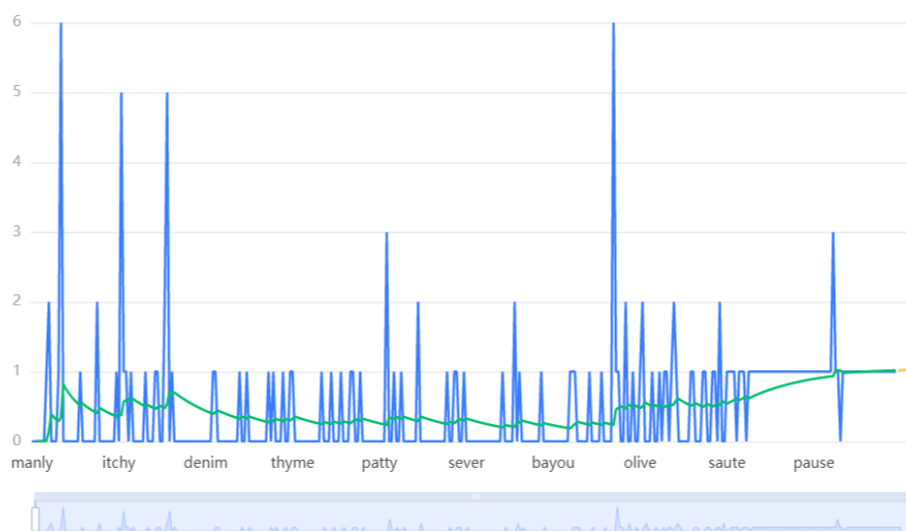
**Figure 5.** Final differential data autocorrelation plot

The system automatically finds the optimal parameters based on the AIC information criterion, and the model results are the ARIMA model (0,0,0) test table based on the variables: 2 tries, and from the analysis of the Q statistic results, we can get: Q6 does not present significance at the level, and the hypothesis that the residuals of the model are white noise series cannot be rejected, while the goodness of fit of the model  $R^2$  is 0.0, and the model performs poorly, and the model basically meet the requirements.

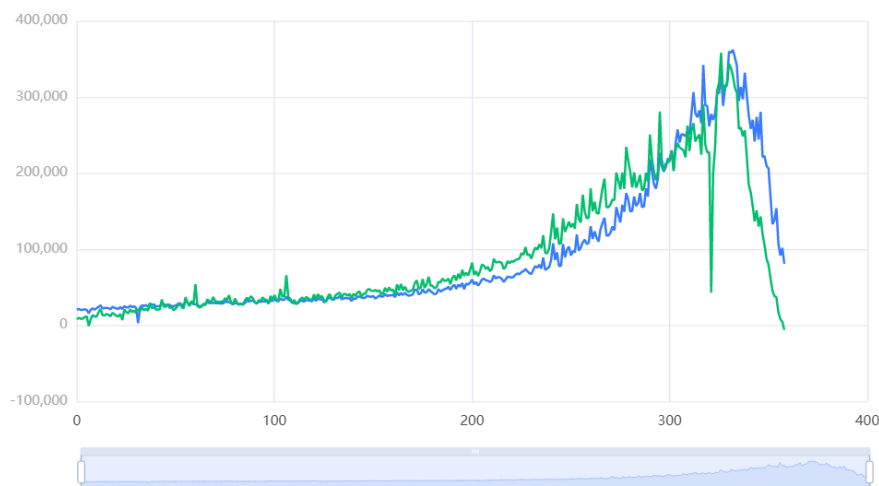
**Table 3.** Table of model parameters

| ARIMA model (0,0,0) test table |              |                |
|--------------------------------|--------------|----------------|
| item                           | Symbols      | Value          |
| Sample size                    | Df Residuals | 358            |
|                                | N            | 359            |
| Q-statistic                    | Q6(P value)  | 0.196 (0.658)  |
|                                | Q12(P value) | 3.551 (0.737)  |
|                                | Q18(P value) | 6.674 (0.878)  |
|                                | Q24(P value) | 9.282 (0.953)  |
|                                | Q30(P value) | 14.136 (0.944) |
| Information Guidelines         | AIC          | 2030.762       |
|                                | BIC          | 2038.529       |
| Goodness of fit                | $R^2$        | 0              |

Note: \*\*\*, \*\*, \* represent 1%, 5%, 10% significance levels, respectively



**Figure 6.** Time series chart

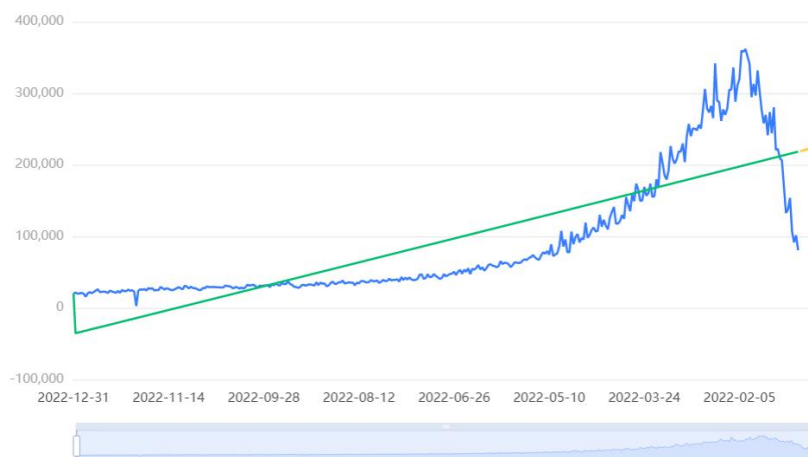


**Figure 7.** Fitting effect graph

The table.4. shows the correct predictions of the time series model for the next seven days for the results of the 2 attempts.

**Table 4.** Time series prediction table

| Predicted value |                   |
|-----------------|-------------------|
| Order (time)    | Predicted results |
| 1               | 5.844011142061282 |
| 2               | 5.844011142061282 |
| 3               | 5.844011142061282 |
| 4               | 5.844011142061282 |
| 5               | 5.844011142061282 |
| 6               | 5.844011142061282 |
| 7               | 5.844011142061282 |



**Figure 8.** Result prediction chart

### 3.1.4 Analysis of results

Taking word characteristics into account as input to the time series prediction model, the tests were related to the attributes of the words. Words with different attributes all reach their highest percentages at a number of attempts of 4, implying that participants encounter different attributes but are most likely to guess the correct answer on the fourth guess at that point. Meanwhile, word frequency and the number of letter repetitions in a word affect the percentage of correct guesses to some extent, with high word frequency being more likely to guess correctly in fewer attempts and low word frequency vice versa. The overall trend for the three cases of letter repetition in words suggests that letter repetition may lead to an increase in the number of attempts people make.

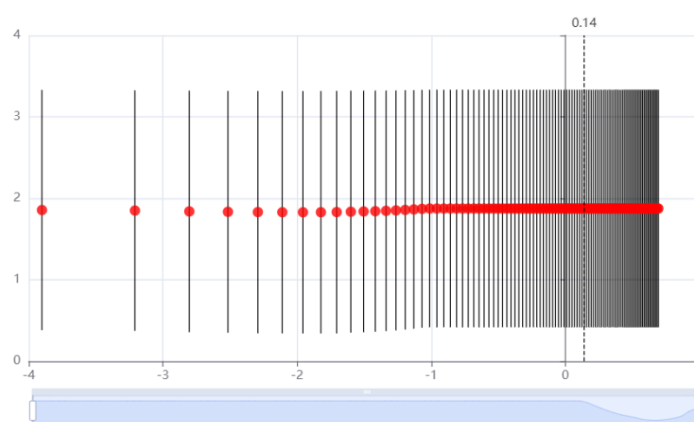
## 3.2. Modeling and solving Problem 2

### 3.2.1 Model Building

Through the cross-validation method, the value of  $\lambda$  was determined.  $\lambda$  values were chosen on the principle that they minimize the mean squared error of the Lasso model. The variables screened by the model are determined through the  $\lambda$  and regression coefficient plots, where the variables with zero standardized coefficients can be considered to be excluded by the Lasso regression model. The equations and prediction cases of the Lasso regression model are obtained and the retained and excluded variables are listed.

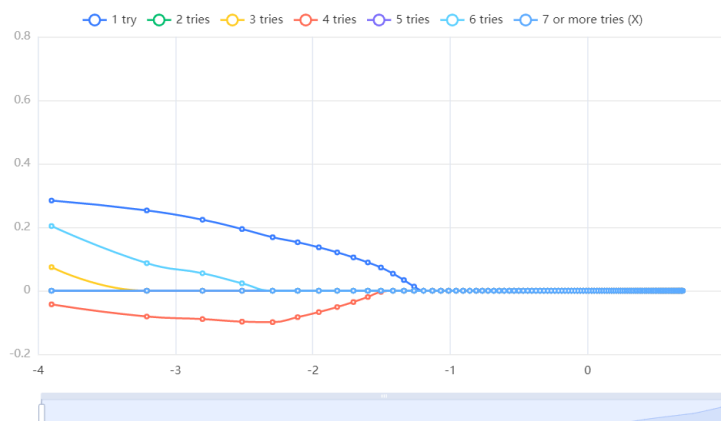
Perform dimensionless processing (homogenization, priming) for the data. Solve the gray correlation coefficient values between the parent series (comparison series) and the feature series. Solve for the gray correlation values. Ranking the gray correlation values and drawing conclusions.

### 3.2.2 Model solving



**Figure 9.** Lasso regression cross-validation plot

To minimize the mean square error determine  $\lambda = 0.141$  and  $\log(\lambda) = -1.956$ .

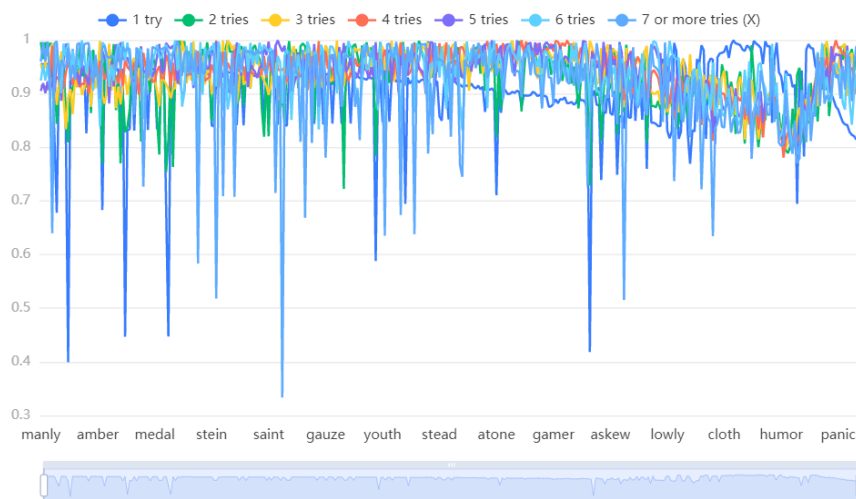


**Figure 10.** Plot of  $\lambda$  vs. model regression coefficients

**Table 5.** Table of model coefficients

| Variable Name       | Standardization factor | Non-standardized coefficient | R <sup>2</sup> |
|---------------------|------------------------|------------------------------|----------------|
| intercept distance  | -12501.516             | -11931.605                   | 0.146          |
| 1 try               | 1381.325               | 1376.849                     |                |
| 2 tries             | 63.389                 | 58.106                       |                |
| 3 tries             | 267.947                | 261.462                      |                |
| 4 tries             | 81.791                 | 77.25                        |                |
| 5 tries             | 166.392                | 159.079                      |                |
| 6 tries             | 306.494                | 302.221                      |                |
| 7 or more tries (X) | 114.135                | 107.796                      |                |

The results of the Lasso regression showed that based on the standardized coefficients of the variable intercept term, 1 try, 2 tries, 3 tries, 4 tries, 5 tries, 6 tries, 7 or more tries (X), the variable intercept term, 1 try, 2 tries, 3 tries, 4 tries, 5 tries, 6 tries, 7 or more tries (X) are retained and no variables are removed.

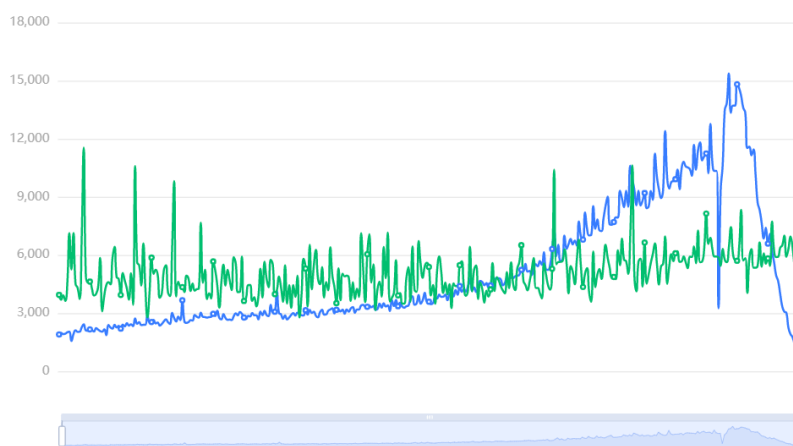


**Figure 11.** Correlation coefficient chart

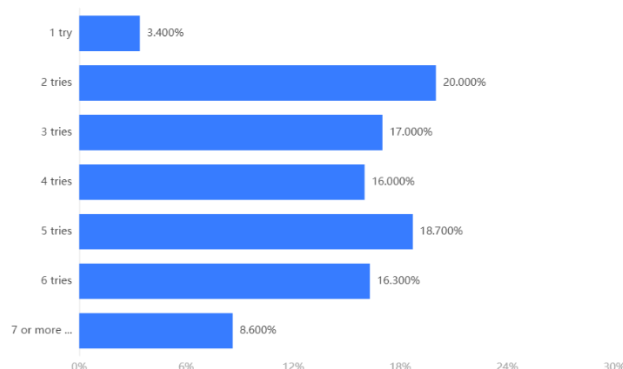
**Table 6.** Relevance ranking

| Relevance results   |           |         |
|---------------------|-----------|---------|
| Evaluation items    | Relevance | Ranking |
| 5 tries             | 0.94      | 1       |
| 4 tries             | 0.938     | 2       |
| 3 tries             | 0.937     | 3       |
| 6 tries             | 0.936     | 4       |
| 2 tries             | 0.929     | 5       |
| 7 or more tries (X) | 0.917     | 6       |
| 1 try               | 0.903     | 7       |

The correlation coefficients were combined with the above correlation coefficients and weighted to obtain the correlation value, which was used to rank the 7 evaluation items; the correlation value ranged from 0 to 1, and the larger the value was, the stronger the correlation with the "reference value" (parent series), which means the higher the evaluation. From the above table, it can be seen that for the seven evaluation items, 5 tries has the highest rating (correlation: 0.94), followed by 4 tries (correlation: 0.938).



**Figure 12.** Model results graph



**Figure 13.** Percentage of feature importance correlation

**Table 7.** Model results predictions

| Variables                  | Coefficient | Test value |
|----------------------------|-------------|------------|
| intercept distance         | 11931.605   | 1          |
| 1 try                      | 1376.849    |            |
| 2 tries                    | 58.106      |            |
| 3 tries                    | 261.462     |            |
| 4 tries                    | 77.250      |            |
| 5 tries                    | 159.079     |            |
| 6 tries                    | 302.221     |            |
| 7 or more tries (X)        | 107.796     |            |
| Forecast result: 12501.516 |             |            |

As can be seen above, the number of attempts needed to guess when the future date is shown above is (3.4%, 20.0%, 17.0%, 16.0%, 18.7%, 16.3%, 5.6%)

The prediction of the term EERIE on March 1, 2023, as shown in the table above, is 125.0516, which is closer to the true value and the predicted value, indicating that the model is accurate and valid.

### 3.3. Modeling and Solving Problem 3

#### 3.3.1 Model Building

First, KMO and Bartlett's tests were performed to determine whether principal component analysis could be performed. For the KMO value: on 0.8 is very suitable for principal component analysis, between 0.7-0.8 is generally suitable, between 0.6-0.7 is less suitable, between 0.5-0.6 indicates poor, and under 0.5 indicates extremely unsuitable. For Bartlett's test, if P is less than 0.05 and the original hypothesis is rejected, it means that principal component analysis can be done, and if the original hypothesis is not rejected, it means that these variables may provide some information independently and are not suitable for principal component analysis. By analyzing the variance interpretation table and the gravel plot, the number of principal components is determined The variance interpretation table mainly looks at the contribution of the principal components to the explanation of the variables (which can be interpreted as how many principal components are actually needed to express the variables as 100%), and if it is too low (e.g., below 60%), the principal component data need to be adjusted. The role of the gravel plot is to confirm the number of principal components to be selected based on the slope of the decline in eigenvalues, and the combination of these two can be used to confirm or adjust the number of principal components. By analyzing the principal component loading coefficients with the heat map, the importance of the hidden variables in each principal component can be analyzed. Based on the principal component loadings map by reducing the dimensionality of multiple principal components into two or three principal components, the spatial distribution of principal components is presented by means of quadrant plots. If 2 principal components are extracted,

the 3D loading principal component scatter plot cannot be presented, and if 1 principal component is extracted, the principal component quadrant plot cannot be displayed. By analyzing the component matrix, the principal component composition formula and weights are derived. The composite score of the principal component analysis method is output.

Clustering category variability analysis based on fields. Analysis of the frequency of each clustering category based on the clustering summary. Based on the dataset clustering annotation can know to which category each sample data is classified. The cluster center coordinates can be used to analyze the distance of each sample from the center point. An overview of the analysis is performed.

### 3.3.2 Model solving

**Table 8.** KMO test and Bartlett's test

| KMO test and Bartlett's test |    |          |          |
|------------------------------|----|----------|----------|
| KMO value                    |    | 0.479    |          |
| Approximate cardinality      |    | 3350.157 |          |
| Bartlett's sphericity test   | df |          | 21       |
|                              | P  |          | 0.000*** |

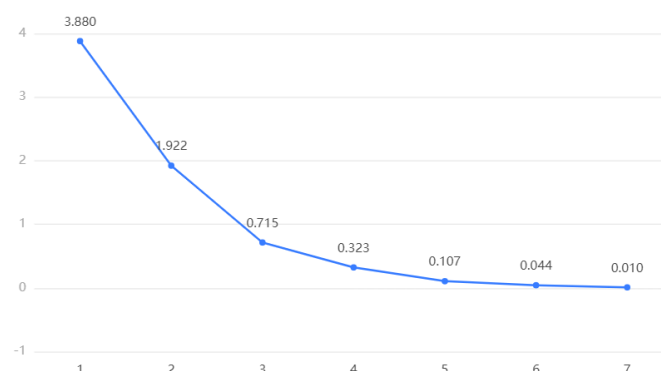
Note: \*\*\*, \*\*, \* represent 1%, 5%, 10% significance levels, respectively

The results of the KMO test showed that the value of KMO was 0.479, while the results of the Bartlett's spherical test showed that the significance p-value was 0.000\*\*\*, presenting significance at the level, rejecting the original hypothesis that there is a correlation between the variables and that the principal component analysis is valid to the extent that it is highly unsuitable.

**Table 9.** Table of explanation of variance

| Ingredients | Total variance explained |                             |                                   |
|-------------|--------------------------|-----------------------------|-----------------------------------|
|             | Feature Root             | Explanation of variance (%) | Cumulative variance explained (%) |
| 1           | 3.88                     | 55.422                      | 55.422                            |
| 2           | 1.922                    | 27.461                      | 82.883                            |
| 3           | 0.715                    | 10.215                      | 93.098                            |
| 4           | 0.323                    | 4.615                       | 97.713                            |
| 5           | 0.107                    | 1.523                       | 99.236                            |
| 6           | 0.044                    | 0.623                       | 99.858                            |
| 7           | 0.01                     | 0.142                       | 100                               |

In the variance explanation table, at principal component 3, the characteristic root of the total variance explained is below 1.0 and the contribution of the variables explained reaches 93.098.



**Figure 14.** Gravel map

**Table 10.** Table of factor loading coefficients

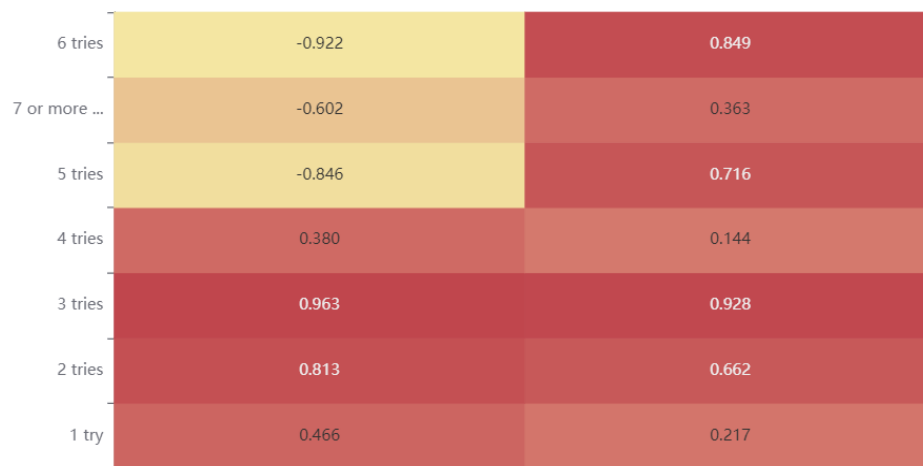
| Factor load factor table |                       |                                      |
|--------------------------|-----------------------|--------------------------------------|
|                          | Factor loading factor | Commonality (common factor variance) |
|                          | Main component 1      |                                      |
| 1 try                    | 0.466                 | 0.217                                |
| 2 tries                  | 0.813                 | 0.662                                |
| 3 tries                  | 0.963                 | 0.928                                |
| 4 tries                  | 0.38                  | 0.144                                |
| 5 tries                  | -0.846                | 0.716                                |
| 6 tries                  | -0.922                | 0.849                                |
| 7 or more tries (X)      | -0.602                | 0.363                                |

**Table 11.** Component matrix

| Component Matrix    |             |
|---------------------|-------------|
| Name                | Ingredients |
|                     | Component 1 |
| 1 try               | 0.12        |
| 2 tries             | 0.21        |
| 3 tries             | 0.248       |
| 4 tries             | 0.098       |
| 5 tries             | -0.218      |
| 6 tries             | -0.238      |
| 7 or more tries (X) | -0.155      |

**Table 12.** Combined score table

| Ranking | Row Index | Overall Score      | Main component 1   |
|---------|-----------|--------------------|--------------------|
| 1       | train     | 2.9149006654696854 | 2.9149006654696854 |
| 2       | plant     | 2.27405950946951   | 2.27405950946951   |
| 3       | slate     | 2.1967500042410357 | 2.1967500042410357 |
| 4       | stair     | 2.13201077506385   | 2.13201077506385   |
| 5       | third     | 2.0610392799765616 | 2.0610392799765616 |
| 6       | dream     | 1.9809406188533856 | 1.9809406188533856 |
| 7       | rainy     | 1.9148765435373374 | 1.9148765435373374 |
| 8       | tash      | 1.9102403888892454 | 1.9102403888892454 |
| 9       | clen      | 1.9034794901482888 | 1.9034794901482888 |
| 10      | alien     | 1.8659820094741104 | 1.8659820094741104 |
| 11      | their     | 1.809402433861196  | 1.809402433861196  |
| 12      | thorn     | 1.7564351155474676 | 1.7564351155474676 |
| 13      | atone     | 1.7558212853010584 | 1.7558212853010584 |
| 14      | treat     | 1.7540260497526905 | 1.7540260497526905 |
| 15      | point     | 1.7531580066458896 | 1.7531580066458896 |



**Figure 15.** Heat map of the factor load matrix

**Table 13.** Field variability analysis

|                     | Clustering categories (mean $\pm$ standard deviation) |                    | F       | P        |
|---------------------|-------------------------------------------------------|--------------------|---------|----------|
|                     | Category 1 (n=202)                                    | Category 2 (n=157) |         |          |
| 1 try               | 0.634 $\pm$ 0.933                                     | 0.261 $\pm$ 0.455  | 21.123  | 0.000*** |
| 2 tries             | 7.901 $\pm$ 4.156                                     | 3.197 $\pm$ 1.831  | 174.65  | 0.000*** |
| 3 tries             | 28.302 $\pm$ 4.762                                    | 15.554 $\pm$ 4.207 | 700.204 | 0.000*** |
| 4 tries             | 34.703 $\pm$ 3.98                                     | 30.643 $\pm$ 6.003 | 59.022  | 0.000*** |
| 5 tries             | 19.861 $\pm$ 3.986                                    | 28.497 $\pm$ 4.296 | 387.225 | 0.000*** |
| 6 tries             | 7.347 $\pm$ 2.465                                     | 16.981 $\pm$ 5.294 | 523.232 | 0.000*** |
| 7 or more tries (X) | 1.173 $\pm$ 0.861                                     | 4.904 $\pm$ 5.491  | 90.48   | 0.000*** |

Note: \*\*\*, \*\*, \* represent 1%, 5%, 10% significance levels, respectively

**Table 14.** Clustering Summary

| Clustering categories | Frequency | Percentage % |
|-----------------------|-----------|--------------|
| Clustering category_1 | 202       | 56.267       |
| Clustering category_2 | 157       | 43.733       |
| Total                 | 359       | 100.0        |

The results of the cluster analysis showed that the clustering results were divided into 2 categories. The frequency of clustering category\_1 is 202, with a percentage of 56.267%. The frequency of clustering category\_2 is 157 and the percentage is 43.733%.

**Table 15.** Data set clustering labeling

| Clustering type | 1 try | 2 tries | 3 tries | 4 tries | 5 tries | 6 tries | 7 or more tries (X) |
|-----------------|-------|---------|---------|---------|---------|---------|---------------------|
| 2               | 0     | 2       | 17      | 37      | 29      | 12      | 2                   |
| 1               | 0     | 4       | 21      | 38      | 26      | 9       | 1                   |
| 2               | 0     | 2       | 16      | 38      | 30      | 12      | 2                   |
| 1               | 0     | 3       | 21      | 40      | 25      | 9       | 1                   |
| 2               | 0     | 2       | 17      | 35      | 29      | 14      | 3                   |
| 2               | 0     | 2       | 8       | 16      | 26      | 33      | 14                  |
| 2               | 1     | 5       | 20      | 35      | 28      | 10      | 1                   |
| 1               | 2     | 11      | 34      | 32      | 15      | 6       | 1                   |
| 1               | 0     | 7       | 26      | 35      | 20      | 10      | 3                   |
| 2               | 0     | 1       | 13      | 34      | 34      | 15      | 2                   |

**Table 16.** Coordinates of clustering centroids

| Clustering type | Center_value_1 try | Center_value_2 tries | Center_value_3 tries | Center_value_4 tries | Center_value_5 tries | Center_value_6 tries | Center_value_7 or more tries (X) |
|-----------------|--------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------------------|
| 1               | 0.6336633663       | 7.90099009           | 28.3019801           | 34.7029702           | 19.8613861           | 7.3465346534         | 1.17326732                       |
|                 | 3663366338         | 90099045             | 98019812             | 970297               | 38613867             | 6534653415           | 67326763                         |
| 2               | 0.2611464968       | 3.19745222           | 15.5541401           | 30.6433121           | 28.4968152           | 16.980891719         | 4.90445859                       |
|                 | 152871             | 9299365              | 2738854              | 01910823             | 8662421              | 745227               | 8726118                          |

**Table 17.** Test data prediction evaluation results

| Predicted results Y | Word   | Predicted outcome probability ty_admit | Predicted outcome probability ty_adore | Predicted outcome probability ty_agape | Predicted outcome probability ty_album | Predicted outcome probability ty_alien | Predicted outcome probability ty_alike | Predicted outcome probability ty_aloud | Predicted outcome probability ty_alpha | Predicted outcome probability ty_ar | Predicted outcome probability ty_angular | Predicted outcome probability ty_ortho | Predicted outcome probability ty_phid | Predicted outcome probability ty_pply |
|---------------------|--------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|-------------------------------------|------------------------------------------|----------------------------------------|---------------------------------------|---------------------------------------|
| applied             | inert  | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0018                                 | 0.0049                                 | 0.0049                              | 0.0049                                   | 0.0049                                 | 0.0049                                | 0.0049                                |
| applied             | olive  | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0018                                 | 0.0049                                 | 0.0049                              | 0.0049                                   | 0.0049                                 | 0.0049                                | 0.0049                                |
| alien               | plan   | 0.0040                                 | 0.0054                                 | 0.0040                                 | 0.0040                                 | 0.0054                                 | 0.0040                                 | 0.0051                                 | 0.0040                                 | 0.0040                              | 0.0040                                   | 0.0040                                 | 0.0040                                | 0.0040                                |
| buggy               | boxide | 0.0042                                 | 0.0016                                 | 0.0042                                 | 0.0042                                 | 0.0016                                 | 0.0042                                 | 0.0029                                 | 0.0042                                 | 0.0042                              | 0.0042                                   | 0.0042                                 | 0.0042                                | 0.0042                                |
| applied             | argof  | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0018                                 | 0.0049                                 | 0.0049                              | 0.0049                                   | 0.0049                                 | 0.0049                                | 0.0049                                |
| caeco               | oye    | 0.0042                                 | 0.0016                                 | 0.0042                                 | 0.0042                                 | 0.0016                                 | 0.0042                                 | 0.0029                                 | 0.0042                                 | 0.0042                              | 0.0042                                   | 0.0042                                 | 0.0042                                | 0.0042                                |
| applied             | flair  | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0049                                 | 0.0010                                 | 0.0049                                 | 0.0018                                 | 0.0049                                 | 0.0049                              | 0.0049                                   | 0.0049                                 | 0.0049                                | 0.0049                                |

|    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |
|----|---|------|------|------|------|------|------|------|------|------|------|------|------|------|
| a  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | m | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | p | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | l |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | e |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | h | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | e | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | e |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | k |      |      |      |      |      |      |      |      |      |      |      |      |      |
| as | h | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| ke | a | 44   | 17   | 44   | 44   | 17   | 44   | 30   | 44   | 44   | 44   | 44   | 44   | 44   |
| w  | m |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | e |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | m | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | i | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | n |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | c |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | e |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | c | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | h | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | u |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | n |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | k |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | r |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | o | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | y | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | a |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | l |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | s |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | q | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | u | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | a |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | d |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | b |      |      |      |      |      |      |      |      |      |      |      |      |      |
| ap | l | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tl | a | 49   | 10   | 49   | 49   | 10   | 49   | 18   | 49   | 49   | 49   | 49   | 49   | 49   |
| y  | c |      |      |      |      |      |      |      |      |      |      |      |      |      |
|    | k |      |      |      |      |      |      |      |      |      |      |      |      |      |

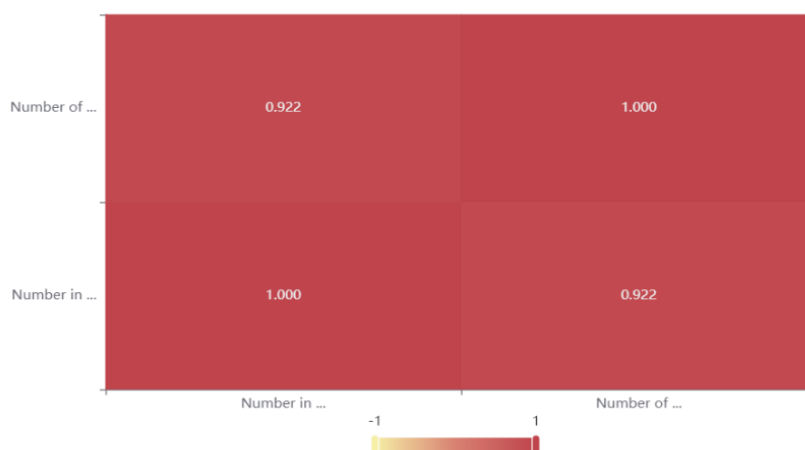
It takes 2 times to predict the word EERIE correctly using the established model, which is efficient. The accuracy is good and the accuracy of the classification model can be obtained from the clustering summary graph.

### 3.4. Modeling and solving Problem 4

The overall descriptive analysis was performed for each statistical indicator of the subgroups.1. The existence of a statistically significant relationship ( $P < 0.05$ ) between XY was first tested. The correlation coefficients were analyzed for the positive and negative directions as well as the degree of correlation. The results of the analysis were summarized.

**Table 18.** Subgroup summary table

| Word  | Number in hard mode | Number of reported results | Contest number | Date    |
|-------|---------------------|----------------------------|----------------|---------|
| abbey | 3345.000            | 132726.000                 | 208.000        | 353.000 |
| admit | 2677.000            | 28994.000                  | 463.000        | 98.000  |
| adore | 2398.000            | 25577.000                  | 533.000        | 28.000  |
| agape | 3671.000            | 43407.000                  | 383.000        | 178.000 |
| ahead | 9396.000            | 203730.000                 | 258.000        | 303.000 |
| album | 4809.000            | 63380.000                  | 339.000        | 222.000 |
| alien | 3395.000            | 38841.000                  | 413.000        | 148.000 |
| alike | 2843.000            | 31277.000                  | 458.000        | 103.000 |
| allow | 8515.000            | 156311.000                 | 273.000        | 288.000 |
| aloft | 13708.000           | 319698.000                 | 231.000        | 330.000 |
| aloud | 2819.000            | 29554.000                  | 502.000        | 59.000  |
| alpha | 2706.000            | 29497.000                  | 451.000        | 110.000 |
| amber | 2261.000            | 23509.000                  | 535.000        | 26.000  |
| ample | 7008.000            | 106681.000                 | 302.000        | 259.000 |
| angry | 3358.000            | 39667.000                  | 395.000        | 166.000 |
| aorta | 2112.000            | 21937.000                  | 552.000        | 9.000   |
| aphid | 3367.000            | 39086.000                  | 397.000        | 164.000 |
| apply | 2150.000            | 22873.000                  | 541.000        | 20.000  |
| apron | 4112.000            | 53430.000                  | 362.000        | 199.000 |
| aptly | 2572.000            | 26498.000                  | 499.000        | 62.000  |
| aroma | 10343.000           | 287836.000                 | 241.000        | 320.000 |
| askew | 6549.000            | 91548.000                  | 310.000        | 251.000 |
| asset | 4733.000            | 63188.000                  | 341.000        | 220.000 |



**Figure 16.** Heat map of correlation coefficient

Using association rules, you can find out which difficulty category a word belongs to if it has the letters E, T, or R, etc.

Based on the relevant data, the characteristics of this data were analyzed in terms of the extreme difference, distribution, anomalies, data volume and data type. The number of reports was found to have a large extreme difference of 359,339, reaching the maximum number of reports and the minimum number of reports on February 2, 2022 and November 30, 2022, respectively. The total number of users suddenly dropped precipitously on November 30, but the number of users in the difficult mode remained almost unchanged, while the number of users in the difficult mode dropped precipitously on February 13, but the total number of users did not differ much from before and after. Such phenomena may be due to incomplete data statistics or increased uncertainty in the number of reports due to social events, holidays, and other external factors.

## 4. Model Evaluation and Extension

### 4.1. Model Evaluation

Advantages of the model are as following.

1. Using the ARIMA model, the iterations are repeated by varying the number of iterations to make the model solution results more accurate and at the same time to check the sensitivity of the results.
2. Under the condition of limited data, a principal component analysis model was used to select the appropriate indicators, and the indicators selected using this model had a more significant impact on the results.
3. A gray correlation prediction model is used to determine the correlation between each indicator, which reduces the correlation between the values of each indicator.

Disadvantages of the model.

1. Some theories in the gray correlation prediction model are not perfect, and some deviations may occur when making predictions.
2. The selection of indicators is made through numerical values in mathematics, without taking into account the actual situation of various indicators appearing in real life.

### 4.2. Promotion of the model

The gray correlation model is usually used to analyze the degree of influence of each factor on the results, and it can also be used to solve comprehensive evaluation problems that change over time.

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