

Gravitational Wave Detection and Its Applications in Multi-Messenger Astronomy

Haoyu Wang

Leicester International Institute, Dalian University of Technology, Panjin, Liaoning, 124221, China
hw370@student.le.ac.uk

Abstract. It ushered in a new era of astronomy with the direct detection of gravitational waves in 2015. A whole new way of stepping into the dark, scary world that Einstein predicted. This paper reviews the theoretical background of gravitational waves and provides an overview of four main categories of primary astrophysical sources, with a particular emphasis on the transient chirp signal. Explanations of principles of detection through laser interferometry, both for those on the ground, LIGO/Virgo, and proposed plans for a space-based version known as the Laser Interferometer Space Antenna (LISA). The gist of this paper is that the first binary black holes, GW150914 in 2015, and the first binary neutron star, GW170817 in 2017, were found. Verifying that the primary origin of heavy elements like gold as well as platinum was the connection between GW and its equivalent EM wave. This was the beginning of multi-messenger astronomy. A brief explanation of astronomical statistics is also provided.

Keywords: Gravitational Waves, Interferometers, Binary Black Hole, Binary Neutron Star.

1. Introduction

The discovery of gravitational waves by indirect observation has opened up an entirely new age of seeing the universe, and will change how people see it directly forever. It has provided a novel messenger, complementing traditional electromagnetic signals. Gravitational waves are old ripples in the most essential stuff in space-time that comes straight from the mass and energy of matter bringing itself together. It gives them the power to see the craziest, wackiest things in space, like big black holes colliding with each other, little stars going boom. Give scientists a special view of places that have very strong gravity, or in places where light cannot be seen from stars that are really, really far away.

This field's theoretical foundations were laid more than a century ago by Albert Einstein. As an important outcome of the general theory of relativity, Einstein predicted the presence of gravitational waves in 1916 [1]. For quite a while, it has been one of the main troubles for experimental physicists. As they had been proved by careful observations of the Hulse-Taylor binary pulsar, but they are still trying to find ways and opportunities for their direct discovery [2]. In 2015, the Advanced Laser Interferometer Gravitational-Wave Observatory (aLIGO) saw GW150914, which was a brief signal from when two black holes had crashed into one another [3]. This was a direct confirmation of Einstein's prediction and it marks the emergence of gravitational wave astronomy as an observational field. In 2017, the discovery of GW170817 brought another great transformation. It was also the first binary neutron star detected at the same time in the gravitational wave and the electromagnetic wave [4]. This multi-messenger event linked such mergers to short gamma-ray bursts, showed these to be chief cosmic locales of heavy nuclei from r processes, and presented new ways to estimate the Hubble constant.

But there's a complication because of the rapid discovery kind. Current ground-based interferometers are plagued by seismic noise and low frequency gravity gradient noise that limits the sensitivity band. In order to overcome the disadvantage above, the Laser Interferometer Space Antenna (LISA) has been designed.

In this paper, according to the basics theory in this paper it reviews some common references and theoretical basics, detection techniques, and discoveries. This essay is aimed to provide a bit of that grand view of GW science, from the basics to revolutionary results. Review of sources theoretical

base and classification of source. Detection technique and facilities is written here, followed by scientific results and discovery, and lastly, prospecting is made in the end.

2. Theoretical Foundation and Generation Mechanisms of Gravitational Waves.

2.1. The Origins of Gravitational Waves

A year after the publication of the general theory of relativity, that is to say in the year 1916, it was Einstein that foretold that an asymmetric change in mass causes an emission of a ripple of energy known as gravitational waves, travelling at the speed of light [1].

The universe's dynamic property generates gravitational waves. According to Einstein's field equations, matter's energy and momentum tell spacetime how to curve. When matter is all mixed up in a super bouncy, time-wiggly way – like when a big star does a huge boom called a supernova, or when two massive things called black holes knock into each other – that bouncy stuff moves out from the middle like when you throw a stone in water and the waves go out. This ripple is a gravitational wave. Creating formula of Gravitational waves, the most classic formula must be the formula of quadrupole, where the wave amplitudes are proportional to the second-time derivative of the source's mass quadrupole moment [5]. In the same category, the mass quadrupole moment is, too, another second-rank symmetric and traceless tensor: the moment theory. Theoretically explains how much does the mass distribution differ from being spherically distributed, and that this is an important topic to study in both Gravitation and Gravity wave study.

2.2. Classifications of Gravitational Waves

Gravitational wave source can be divided into 4 types according to the source's waveform characteristics. Gravitational waves sources are mainly transient chirp-type sources, Continuous monochromatic sources, noisy stochastic background sources, and burst sources. [5]

Type one is chirp signal. This is currently the most recognized, and most successful, form of resource identification, with a clear origin coming from binary black hole/binary neutron star/Black Hole-Neutron Star systems. The orbiting binary system releases gravitational waves to lose orbital energy during the first inspiral phase. The objects spiral inward as a result of this energy loss, which lowers orbital separation and raises the frequency and amplitude of the gravitational wave signal. This is followed by the merger phase, where the two objects collide and coalesce, and the waveform reaches its peak amplitude. Finally, there is the ring-down phase, where the newly created item undergoes rapid oscillations that quickly damp out. This signal directly reveals properties of the compact objects like their spins and masses.

Continuous gravitational waves, the stochastic gravitational-wave background, and burst sources represent three other important categories of sources of gravitational waves. Non-axisymmetric and rapidly rotating neutron stars are predicted to produce continuous gravitational waves, which are characterized by an almost constant frequency and extremely long-lasting, quasi-monochromatic signals. A random signal, which is known as the stochastic gravitational-wave occurrences, is produced by the superposition of several indistinguishable separate gravitational-wave occurrences, such as those from cosmic inflation or distant binary coalescences, manifesting as an isotropic stochastic process. Burst sources refer to brief signals originating from unpredictable transient events, like core-collapse supernovae, featuring non-repeating and uncertain waveforms. The detection of these signals will be used to study neutron star internal structure, early universe physics, and extreme astrophysical processes, respectively.

3. Detection Techniques and Facilities

3.1. The principles of detection and Challenges

Laser interferometry serves as the foundational technology to directly detect gravitational waves. The principle of an interferometric detector, like LIGO, includes dividing a laser beam into two beams, which propagate respectively in two vertical long arms and are reflected back by the end reflector. Two Light beams meet and again, when there is a difference in Optical Path, Interference Fringes would show up. In a calm state, stripes are still. The gravitational waves pass through the detector, one gets stretched and the other gets squished in an unbalanced way, and that changes the total time each single beam of light takes to travel, so it shifts the places along the screen where the two columns of light stripes meet up with each other. As for the job of the detector: It's to watch those stripes that are tiny.

The unique advantages of laser interferometers are multifaceted. Firstly, they can achieve extremely high sensitivity across a broad frequency range, sufficient to detect the minute physical strain induced by gravitational waves [6]. Secondly, the test masses are suspended as pendulums and are widely separated; this configuration can effectively isolate seismic noise and mitigate the effects of thermal noise, allowing the motion of the masses to be driven more purely by gravitational waves [6]. Finally, the structure of the Michelson interferometer is inherently well-suited to the quadrupolar nature of gravitational waves [6].

However, the challenge is that the relative arm length variation (strain) caused by gravitational waves is as small as the order of 10^{-21} [3]. This means that the four-kilometer LIGO arm changed by 4×10^{-18} meters [7]. To detect such small signals, LIGO must overcome various noises far more powerful than the signals, which requires a series of revolutionary technologies.

3.2. Laser Interferometers

In this section, four core techniques will be introduced briefly by taking Advanced Virgo as an example.

First, the paper will introduce the most critical technology on the interferometer arms: the Fabry–Pérot cavity. Each arm of Advanced Virgo consists of a three-kilometer-long Fabry–Pérot cavity. The laser light reflects multiple times between the input mirror and the end mirror, accumulating light intensity and amplifying the phase shift caused by gravitational waves. Furthermore, its adoption of a bi-concave, nearly confocal geometric structure can reduce noise interference and radiation pressure instability.

Second is the power recycling technology, which consists of two parts: the power recycling cavity and the thermal compensation system. The former can circulate and enhance the laser power in the arms, up to a maximum of 700 kW, reducing quantum noise [8]; the latter can reduce coupling losses to the parts-per-million (ppm) level, ensuring the detector can operate stably at high power [8].

Three is the Suspension and vibration isolation system consisting of super attenuator (isolated vibration support), a Mono monocrystalline suspension fiber (noise reduction and interference resistance), and active control (adjust position, control vibration). Vibration isolation, noise reduction and stable detection are also its functions.

Finally came the vacuum system The entire interferometer has to be in a ultra-high vacuum, around $7,000\text{m}^3$, so you have to control the noise by controlling the pressure, and you have to cool it with large cryogenic traps, to preserve purity and stability in the optical path.

3.3. Future Technology—LISA

Ground-based interferometers still have limitations. They are constrained by seismic noise and gravity gradient noise, making them insensitive to low-frequency gravitational waves (below 10 Hz). The Laser Interferometer Space Antenna (LISA) takes the stage in response to this requirement. The European Space Agency (ESA) is leading the project, and NASA is involved. LISA is expected to launch in the mid-2030s. In orbit, three spacecraft with arm lengths of 2.5 million kilometers will

form a huge equilateral triangle [9]. By measuring minute changes in laser beams between the spacecraft over these unparallel long baselines, LISA will detect gravitational waves in the frequency range of 0.1 mHz to 1 Hz, enabling people to observe cosmic events such as mergers of supermassive black holes [9].

4. Key Scientific Results and Discoveries of GWs

The fundamental evidence that GWs exist is their direct detection which was only achieved in 2015. The direct detection of GWs by advanced LIGO in 2015 (GW150914) was a groundbreaking breakthrough in physics [3]. It not only conclusively validates Einstein's prediction but also pushes gravitational-wave astronomy from a field of confirmatory pursuit to a vibrant, discovery-driven discipline. Soon after, the 2017 detection of the binary neutron star merger (GW170817) laid the foundation for multi-messenger time-domain astronomy. This section reviews the key discoveries that defined this new era.

4.1. Case one—a Binary Black Hole Merger

At 09:50:45 UTC on September 14, 2015, a gravitational-wave (GW) signal was detected by the LIGO observatories located in Hanford, Washington, and Livingston, Louisiana [3]. The signal was subsequently verified to have a false-alarm-probability of being caused by random noise fluctuations of less than 2×10^{-7} [3]. The signal originated from the merger of two black holes located approximately 410^{+160}_{-180} Mpc (about 1.3 billion light-years) from Earth [3]. The primary black hole had a mass of $36^{+5}_{-4}M_{\odot}$, while the secondary had a mass of $29^{+4}_{-4}M_{\odot}$. They combined to create a final black hole of $62^{+4}_{-4}M_{\odot}$, thereby releasing energy equivalent to $3^{+0.5}_{-0.4}M_{\odot}$ in gravitational waves [n].

The significance of this discovery even extends further. Prior observations indicated that any stellar-mass black hole in the Galaxy had a maximum mass of about $15 M_{\odot}$. GW150914 not only confirmed the existence of stellar-mass black holes exceeding about 25 solar masses (M_{\odot}) but also established that binary black holes can form in nature and merge within a Hubble time [3]. In other words, this single detection more than quadrupled the known mass range for stellar-mass black holes.

What also mattered was GW150914's validation of General Relativity in the strong-field regime. The event passed three consistency tests. First, using numerical relativity simulations, the mass and spin of the remnant black hole were checked for consistency with the predictions from the initial black holes [10]. Second, relying on the post-Newtonian formalism, the consistency between the observed data and the 'deviated waveform' (a waveform model incorporating potential deviations from General Relativity) was tested via the phase evolution of the gravitational waveform [10]. Third, the dispersion relation of gravitational waves was tested. General Relativity predicts a massless graviton, resulting in a linear dispersion relation; a massive graviton would modify this relation. Ultimately, the results from all three tests demonstrated that GW150914 is in complete agreement with the predictions of General Relativity in the strong-field regime [3].

In addition to the more important GW150914 detection. More importantly, the detection of GW150914 means that there is a new domain, i.e., studying the population, the production and evolution history of compact objects with gravitational wave signals, which can be called gravitational-wave astrophysics. It produces new issues and restrictions for models of growing stars.

4.2. Case 2—a Binary Neutron Star Inspiral

On August 17, 2017 at 12:41:04 UTC: Another huge milestone: The Advanced LIGO and Advanced Virgo detectors observed the first directly detected binary neutron star inspiral [4]. It's the point at which the binary system starts to radiate away its energy gravitationally, and the two stars start spiralling in towards each other. The signal was given the label GW170817, and its calculated FAR of <1 per 80000 years means it's not likely a false positive [4].

The source was bound to an area of the sky that was 28 square degrees with 90%CL, which was the most precise localization of a GW signal up until that point. Its distance was estimated to be approximately 40_{-14}^{+8} MPC from Earth, also making it the closest detected event [4]. Afterwards, about 1.7seconds later, the Fermi Gamma-ray Burst Monitor (GBM) detected and triggered on a short gamma-ray burst (GRB), which was GRB 170817A [11].

This thing has quite a lot to it; it's shown through different parts, first about the reasons behind short-duration gamma ray bursts less than two seconds, which was hard to understand in space science. This kind of detection makes it absolutely clear that two neutron stars colliding with one another is likely the cause of at least part of the brief gamma-ray bursts.

Second, theories show that when they come together, these pairs of stars produce a fast process that makes heavy elements (R-process), which could be responsible for making up a lot of what is heavy in our universe [12]. After the detection of optical/infrared radiation, which matches exactly with the luminosity, color, and evolution of the “kilonova” model, was the first direct confirmation [13]. The radioactive decay of the r-process components is exactly what propels a kilonova. So, it should be verified for the record that it does, in fact, produce gold, platinum, and all the other good stuff to be put back into the universe.

In addition to that on another side, which was deeper, it was an outstanding demonstration of multi-messenger astronomy. For this event, the observed gravitational-wave signal is an estimate of the luminosity distance [4]; simultaneously observing things optically gave scientists the host galaxy (NGC 4993), its redshift (and hence its recession velocity) [4]. And then it's also possible for a simple observational estimation of the Hubble constant as well. Use absolute distance to the gravitational wave source, which is obtained upon detection [14]. It might be only on account of a single activity, but it does showcase that this approach can be successful, and it brings about a new way to calculate the Hubble Constant.

This is the first gravitational wave detection where electromagnetic signals were also received from the source. This opens up a new era for so-called multi-messenger astronomy. As an example, they performed a series of “null tests” to test whether general relativity still holds true in extreme regimes of gravity, i.e., whether the data matches the predictions of GW [15].

5. Conclusion

The discovery of gravitational waves is undoubtedly an era in the world of astronomy. It reviews its development from the theoretical basis in Einstein's general Relativity to a central part of observational astrophysics today. The 4 astrophysical sources of gravitational waves have been distinguished clearly. Laser interferometry's detection principles followed this. LIGO, Virgo, and KAGRA – the engineering monuments that allows people to actually see those mysterious ripples in spacetime itself – appeared. Confirming the binary black hole mergers GW150914 and its consistency with both strong-field tests of general relativity and the historic binary neutron star merger GW170817 which marked the advent of multi-messenger astronomy is the most important step.

As far as moving forward, GW science has an even bigger blue print. With more and more data observed, the method of utilizing gravitational waves is progressively transforming the isolated analysis into statistical astrophysics, which investigates the overall populations of cosmic objects, such as the mass and spin distributions of black holes and neutron stars. It to some degree gives scientists some ideas and some limits on how they think black holes and neutron stars were formed and what happened to them throughout their time in the universe. In the future, The Cosmic Explorer and Einstein Telescope constitute the next generation of ground-based detectors, which will have great increase in statistical analysis capabilities. And it will be more sensitive many times over than anything existing today. At the same time, the planned space-based mission LISA will also provide a new window of observation at the low-frequency end of the gravitational wave band.

In summary, gravitational wave astronomy is no longer a method to verify existing theories but a powerful tool for discovering the unknowns in the cosmos. In the future, it is expected to become the

fundamental rules of the universe, which can help scientists research the extreme phenomena in the universe.

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